

Review Homework

1. Section 5.5
2. ~~10~~, ~~24~~
3. Use Part 1 of the Fundamental Theorem of Calculus to find the x -derivative of the function
10. $h(x) = \int_0^x \sqrt{1+r^3} dr$
6. Find the interval on which the curve
 $y = \int_0^x \frac{1}{1+t+t^2} dt$ is concave upward.

8.2

15. Determine whether the series converges.

$$\sum_{n=1}^{\infty} \sqrt[n]{2}$$

27. Find the values of x for which the series converges.

$$\sum_{n=1}^{\infty} \frac{1}{3^n}$$

Blake Oliaro
12-9-09

1. $\int_{\pi/2}^{\pi} x^3 \cos(x^2) dx$

2. $\int_0^{1/2} \sin^{-1}(x) dx$

Find the Remainder at $n=8$

8.4 Alternating Series Remainder

$$\boxed{7} \sum_{n=1}^{\infty} (-1)^n \frac{3n-1}{2n+1}$$

$$\boxed{8} \sum_{n=1}^{\infty} (-1)^{n-1} \frac{\ln n}{n}$$

Eli Scandalis

Determine whether the series is absolutely conv., condit. conv., or diverges.

$$1) \sum_{n=1}^{\infty} \left(\frac{n^2+1}{2n^2+1} \right)^n$$

$$2) \sum_{n=1}^{\infty} \frac{(-1)^n}{(\arctan n)^n}$$

Review Problems

1. A spring has a natural length of 20 cm. If a 25 N force is required to keep it stretched to a length of 30 cm, how much work is required to stretch it from 20 cm to 30 cm?

2. If 6 J of work is needed to stretch a spring from 10 cm to 12 cm and another 10 J is needed to stretch it from 12 cm to 14 cm, what is the natural length of the spring?

Alison Mackey

1. $\int x e^{x^2} dx$

2. $\int_0^{\pi} \sec^2(t/4) dt$

David Vandell

6.4 (Tables of Integrals)

Find the following integrals, using table of integrals:

1. $\int e^{2x} \sin(3x) dx$

2. $\int \frac{\sqrt{5x+23}}{x^6} dx$

Converge or Diverge?

$$\textcircled{1} \sum_{n=0}^{\infty} \frac{n^2}{5n^2 + 4}$$

Converge or Diverge?

$$\textcircled{2} \sum_{n=1}^{\infty} \frac{1}{n}$$

Kevin Forey

Determine if convergent

or divergent:

$$\sum_{n=1}^{\infty} \frac{1}{\sqrt{n^2+1}}$$

Jacob
R.

8.7

$$f(x) = e^{i\theta}$$

$$f(x) = e^{i\frac{\theta}{b}}$$

REVIEW PROBLEMS

1. Determine whether the series is absolutely convergent, conditionally convergent, or divergent

$$\sum_{n=1}^{\infty} \frac{(-3)^n}{n^3}$$

2. (a) show that $\sum_{n=0}^{\infty} \frac{x^n}{n!}$ converges for all x
(b) deduce that $\lim_{n \rightarrow \infty} \frac{x^n}{n!} = 0$ for all x

Beau Island Questions

1. Is the following series convergent or divergent? If it is convergent, find what it converges to.

$$1 + 0.4 + 0.16 + 0.064 + \dots$$

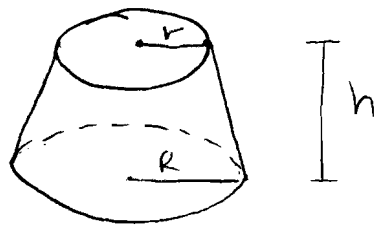
2. Does the following series converge? If so, what does it converge to?

$$\sum_{n=1}^{\infty} \frac{1+3^n}{2^n}$$

1. Find the volume of the solid obtained by rotating the region bounded by the given curves about the specified line. Sketch the region, the solid, and a typical disk or washer.

$$y = \frac{1}{x}, x = 1, x = 2, y = 0; \text{ about the } x\text{-axis}$$

2. Find the volume of a frustrum of a right circular cone with height h , lower base radius R , and top radius r .



Will Muldoway

$$2. \int \sin^6 x \cos^3 x dx$$

$$32. \int \csc^4 x \cot^6 x dx$$

Maddie Gerling

1) Evaluate $\int x \tan^2 x$ to the 4th decimal

2) Find the Maclaurin series for $f(x) = x \cos^2 x$

Ian Mahaney

Evaluate the integrals:

$$\textcircled{A} \int_0^1 \frac{2x+3}{(x+1)^2} dx$$

$$\textcircled{B} \int \frac{5x^2+3x-2}{x^3+2x^2} dx$$

7.1

Sketch the region enclosed by the given curves. Decide whether to integrate with respect to x or y . Draw a typical approximating rectangle and label its height and width. Then find the area of region.

1) $y = x + 1$, $y = 9 - x^2$, $x = -1$, $x = 2$

2) $y = \sin x$, $y = 2x/\pi$, $x \geq 0$

Ally Mucci♥

7) Find the derivative of the function.

$$g(y) = \int_2^y t^2 \sin(t) dt$$

13) Find the derivative of the function.

$$g(x) = \int_{2x}^{3x} \frac{u^2 - 1}{u^2 + 1} du$$

Section 8.3 (P-Series) - Review Questions

Determine whether the series is convergent or divergent:

$$(20) \sum_{n=1}^{\infty} \frac{1}{\sqrt{n^3+1}}$$

$$(26) \sum_{n=1}^{\infty} \frac{n+5}{\sqrt[3]{n^7+n^2}}$$

Kristin Crawford

12/9/09

$$7. \sum_{n=1}^{\infty} \frac{1}{n^4}$$

$$25. \sum_{n=1}^{\infty} \sin\left(\frac{1}{n}\right)$$

Find a formula for the general term a_n of the sequence, assuming that the pattern of the first few terms continues.

$$\left\{ 1, -\frac{2}{3}, \frac{4}{9}, -\frac{8}{27}, \dots \right\}$$

Determine whether the sequence converges or diverges. If it converges, find the limit.

$$a_n = \frac{(-1)^n n^3}{n^3 + 2n^2 + 1}$$

Find the radius of convergence and the interval of convergence of the series.

$$16 \sum_{n=1}^{\infty} \frac{n(x-4)^n}{n^3+1}$$

$$17 \sum_{n=1}^{\infty} n!(2x-1)^n$$

Problems

1. Find the power series representation of the function and the interval of convergence.

$$f(x) = \frac{x}{9+x^2}$$

2. Use a power series to approximate the definite integral to six decimal places.

$$\int_0^{0.3} \frac{x^2}{1+x^4} dx$$

"Volumes by Cylindrical Shells"

#1 Use the method of cylindrical shells to find the volume generated by rotating the region bound by,

$y = x^2$, $y = 0$, $x = 1$
about the y -axis.

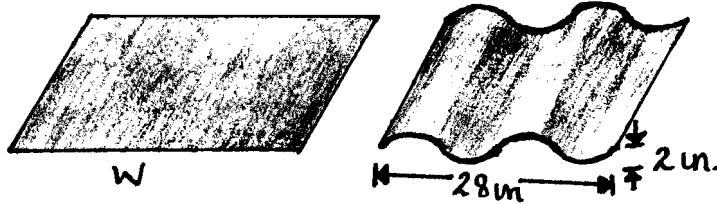
#2 Use cylindrical shells to find the volume of the region bounded by

$x = y^2$
and $y = x - 2$
around $y = -2$

1. Find the arclength.

$$y = \ln(\cos x) \quad 0 \leq x \leq \frac{\pi}{3}$$

2. A manufacturer of corrugated metal roofing wants to produce panels that are 28 in. wide and 2 in. thick by processing flat sheets of metal as shown below. The profile of the roofing takes the shape of a sine wave. Verify that the sine curve has the equation $y = \sin(\pi x/7)$ and find the width, w , of a flat metal sheet used to make the panel. (Use your calculator to evaluate the integral to four significant figures)



5.1 : Areas & Distances.

Erin Hong
Calc II

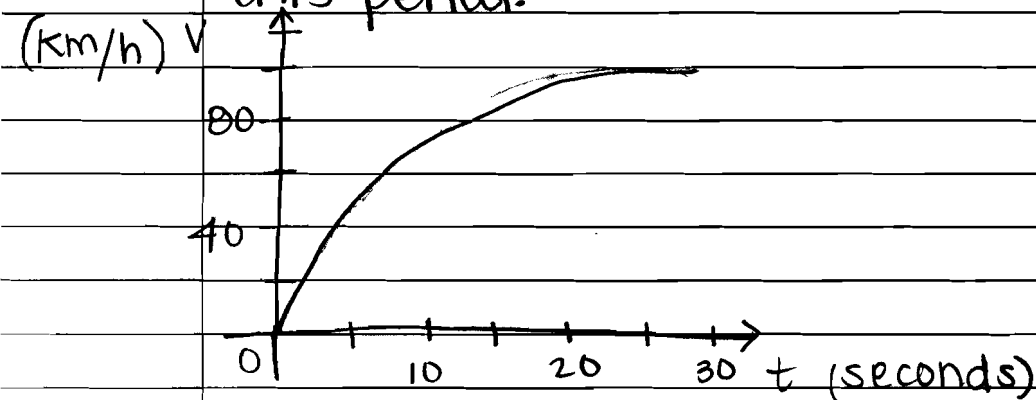
3.

a. Estimate the area under the graph of $f(x) = 1/x$ from $x=1$ to $x=5$ using four approximating rectangles and right endpoints. Sketch the graph and the rectangles. Is your estimate an underestimate or an overestimate?

b. Repeat part (a) using left endpoints.

5.1: Areas & Distances

12. The velocity graph of a car accelerating from rest to a speed of 120 km/h over a period of 30 seconds is shown. Estimate the distance traveled during this period.



Daniel Hagen

Question #1

Determine whether the series is absolutely convergent, conditionally convergent, or divergent.

$$\sum_{n=1}^{\infty} \left(\frac{(n^2 + 1)}{(2n^2 + 1)} \right)^n$$

Question #2

Determine whether series is absolutely convergent, conditionally convergent, or divergent.

$$\sum_{n=1}^{\infty} (-1)^n \left(\frac{n}{n^2 + 1} \right)$$

HW# 48

35. Determine whether the integral is convergent or divergent.
Evaluate if convergent.

$$\int_{-2}^{14} \frac{dx}{\sqrt[4]{x+2}}$$

1. Explain why each of the following integrals is improper.

a) $\int_1^{\infty} x^4 e^{-x^4} dx$

b) $\int_0^{\pi/2} \sec x \cdot dx$

c) $\int_0^2 \frac{x}{x^2 - 5x + 6} dx$

d) $\int_1^2 \ln(x-1) dx$

1) Find the area between the curves $y=12-x^2$ and $y=x^2-6$

2) Find the area between the curves $y=x^2-x$ and $y=x^3-4x^2+3x$

Ellen Stidham

$$\int_0^{\pi/4} \frac{1 + \cos^2 \theta}{\cos^2 \theta} d\theta$$

$$\int_{-1}^0 (2x - e^x)$$

Kate
Partynski

1) Approximate the given integral using:

a) The midpoint Rule

b) The Trapezoidal Rule

c) Simpson's Rule

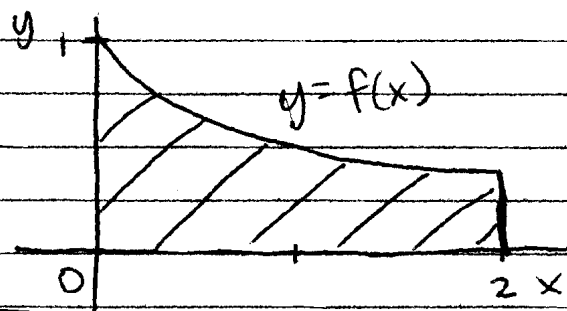
$$\int_1^2 \frac{1}{x} dx$$

and 4 intervals.

2) The left, Trapezoidal, and Midpoint Rule approximations were used to estimate $\int_0^2 f(x) dx$ (the graph of f is shown). The estimates were 0.7811, 0.8675, 0.8632, and 0.9540. The same number of sub-intervals was used in each.

a) Which rule produced which estimate?

b) Between which two approximations is the true value of $\int_0^2 f(x) dx$?



- 1) Assume a demand curve $p_d(x) = -0.1x^2 - 10x + 200$.
- what price should the producer charge to maximize revenue?
 - what is the consumer surplus at this price?
- 2) The demand function for a certain commodity is $p = 5 - \frac{1}{10}x$. Find the consumer surplus when the sales level is 30. Draw the demand curve & identify the consumer surplus.

13) Find the Taylor series for $f(x)$ centered at the given value of a . Find the radius.

$$f(x) = e^x, a = 3$$

44) Evaluate the indefinite integral as an infinite series.

$$\int \frac{\sin x}{x} dx$$

$$\int_0^{\pi/3} \tan^5 x \sec^4 x \, dx$$

$$\int_0^{2\sqrt{3}} \frac{x^3}{\sqrt{16-x^2}} \, dx$$

8.3 Direct Comparison Test

9.

$$\sum_{n=1}^{\infty} \frac{1}{n^2 + n + 1}$$

21.

$$\sum_{n=1}^{\infty} \frac{1}{\sqrt{n^2 + 1}}$$

Juggan Clem

Section ██████

0) Express the limit as a definite integral on the given interval.

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{e^{x_i}}{1+x_i} \Delta x \quad [1, 5]$$

1) Evaluate the integral

$$\int_0^2 (2-x^2) dx$$

Heidi Hirsh

49. $\int_0^{0.1} \frac{dx}{\sqrt{1+x^3}}$ (|error| $< 10^{-8}$)

51. $\lim_{x \rightarrow 0} \frac{x - \tan^{-1} x}{x^3}$

Final Review:

12/09/09

Chapter 6.1

7. evaluate the integral (by parts)

$$\int x^2 \sin \pi x \, dx$$

26 $\int x^5 \cos(x^3) \, dx$