

Homework 1

These problems are to get you to look back at your calculus 1 notes and see if you can remember how to do them. You could also get a calculus 1 textbook for help.

1. Let

$$f(x) = \frac{5x^3 + 3\sqrt{x}}{x}$$

find $f'(x)$.

2. Find

$$\frac{d}{dx} \sqrt{5x^2 + \sqrt{x}}$$

3. Find the equation of the tangent line of:

$$y = \cos(x) + \sin(x)$$

at $(\frac{\pi}{4}, \sqrt{2})$ and $(\frac{\pi}{3}, \frac{\sqrt{3}+1}{2})$

4. If the position of a particle at time t is given by:

$$s(t) = \sqrt{t}e^t$$

find the acceleration of the particle at time $t = 4$.

Answer:

$$\frac{79}{32}e^4$$

5. $D_x(2^{x^2+1})$

6. $D_x(\ln(\sin(\tan(x))))$

Note $D(\tan(x)) = \sec^2(x) = 1 + \tan^2(x)$.

7. Sketch a graph of a function that satisfies the following table. Note one of the f'' is impossible, figure out which one is impossible and eliminate it.

| | $x \leq 1$ | $1 \leq x \leq 2$ | $2 \leq x \leq 3$ | $3 \leq x \leq 4$ | $x \geq 4$ |
|----------|------------|-------------------|-------------------|-------------------|------------|
| f | - | + | + | + | + |
| f' | + | + | - | - | + |
| f'' | + | + | + | - | - |
| or f'' | - | - | - | + | + |