## Math 310 <br> Assignment \# 1

1. For each of the following find all solutions to the system of equations do the following: i) write down the coefficient matrix for the system, ii) write down the augmented matrix for the system, iii) do Gauss-Jordan elimination on the augmented matrix, iv) use the previous part to write down a solution set for the system of equations
(a)

$$
\begin{aligned}
& 3 x+6 y-3 z=9 \\
& 2 x-2 y-2 z=1
\end{aligned}
$$

(b)

$$
\begin{aligned}
2 x_{1}+2 x_{4} & =6 \\
x_{1}+x_{2}+x_{3}+x_{4} & =7 \\
3 x_{3}+3 x_{4} & =1
\end{aligned}
$$

(c)

$$
\begin{aligned}
3 x_{1}+2 x_{2}+3 x_{3}-x_{4} & =1 \\
3 x_{1}+x_{3}+4 x_{4} & =20 \\
3 x_{1}+x_{3}-3 x_{4} & =11 \\
2 x_{1}-2 x_{2}+x_{3}+4 x_{4} & =14
\end{aligned}
$$

2. Let $A$ and $B$ be $n \times n$ matrices.
(a) Use the distributive law (twice) to expand the quantity $(A+B)(A-B)$.
(b) Explain why $(A+B)(A-B)$ need not equal $A^{2}-B^{2}$ (as it does for real numbers).
