## Math 320 Linear Algebra Assignment # 8

1. Let A be as follows:

	Γ0	0	2	-4	8	2/5	-4/5]
	0	2	-2	6	4	18	2
A =	0	4	-4	12	9	33	5
	0	4	-4	12	8	37	2
	0	0	5	-10	20	1	-2

Find:

- (a) A basis for col(A).
- (b) A basis for row(A).
- (c)  $\operatorname{rank}(A)$
- (d) if each of  $\vec{b}_1, \vec{b}_2, \vec{b}_3$  is in col(A) or row(A) (could be in one of them, both or neither):

$$\vec{b}_1 = \begin{bmatrix} -96/5\\58\\102\\118\\-48 \end{bmatrix}, \vec{b}_2 = \begin{bmatrix} 1\\1\\0\\1\\0 \end{bmatrix}, \vec{b}_3 = \begin{bmatrix} 0\\8\\-22\\52\\-39\\346/5\\43/5 \end{bmatrix}$$

2. Suppose  $\vec{r_1}, \vec{r_2}, \ldots, \vec{r_m} \in V$  and  $\alpha \in \mathbb{R}$  and  $1 \leq i, j \leq n$  with  $i \neq j$ . Show that the

 $\operatorname{span}(\vec{r_1}, \vec{r_2}, \dots, \vec{r_i}, \dots, \vec{r_j}, \dots, \vec{r_m}) = \operatorname{span}(\vec{r_1}, \vec{r_2}, \dots, \vec{r_i}, \dots, \vec{r_j} + \alpha \vec{r_i}, \dots, \vec{r_m}).$ 

This show that a the row space does not change when the third type of elementary row operation is performed. (Notice that you are proving something stronger since you are showing it for every vector space not just  $\mathbb{R}^{n}$ .)

3. Determine if the following square matrices are singular or nonsingular.

$$A_{1} = \begin{bmatrix} 3 & -2 & -3 \\ 0 & 2 & -3 \\ -1 & 3 & -3 \end{bmatrix}$$
$$A_{2} = \begin{bmatrix} 1 & 5 & 2 & 15 \\ -1 & 0 & -1 & 1 \\ 3 & -3 & 1 & -14 \\ 5 & 3 & 0 & -1 \end{bmatrix}$$
$$A_{3} = \begin{bmatrix} 2 & 1 & 2 & 0 & 2 & 0 \\ 2 & 0 & 2 & 1 & 1 & 2 \\ 1 & 0 & 1 & 1 & 1 & 1 \\ 2 & 1 & 1 & 0 & 2 & 2 \\ 1 & 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 2 & 1 & 2 & 0 \end{bmatrix}$$

4. Given  $a, b, c \in \mathbb{R}$  with  $a \neq 0$  find d so that  $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$  is singular.