

Math 320 Linear Algebra Assignment # 5

1. Consider the set of vectors, $\{\vec{v}_1, \vec{v}_2, \vec{v}_3, \vec{v}_4, \vec{v}_5, \vec{v}_6\}$. Suppose that the matrix:

$$A = [\vec{v}_1 \ \vec{v}_2 \ \vec{v}_3 \ \vec{v}_4 \ \vec{v}_5 \ \vec{v}_6]$$

is row equivalent to

$$\begin{bmatrix} 3 & 2 & -1 & 3/2 & -1 & 5 \\ 0 & 2 & 1 & 2 & 3 & 1 \\ 0 & 0 & 0 & 3/7 & -4 & 8 \\ 0 & 0 & 0 & 0 & 0 & 16 \end{bmatrix}.$$

- (a) Is $\{\vec{v}_1, \vec{v}_2, \vec{v}_3, \vec{v}_4, \vec{v}_5, \vec{v}_6\}$ linearly independent or dependent?
- (b) Is $\{\vec{v}_1, \vec{v}_2\}$ linearly independent or dependent?
- (c) Is $\{\vec{v}_1, \vec{v}_2, \vec{v}_3\}$ linearly independent or dependent?
- (d) Is $\vec{v}_3 \in \text{span}(\vec{v}_1, \vec{v}_2, \vec{v}_4, \vec{v}_5, \vec{v}_6)$?
- (e) Is $\vec{v}_3 \in \text{span}(\vec{v}_1, \vec{v}_2)$?
- (f) Is $\vec{v}_4 \in \text{span}(\vec{v}_1, \vec{v}_2, \vec{v}_3)$?
- (g) Is $\vec{v}_5 \in \text{span}(\vec{v}_1, \vec{v}_2, \vec{v}_3, \vec{v}_4)$?
- (h) Let

$$\vec{u} = \begin{bmatrix} 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}.$$

Is $\vec{u} \in \text{span}(\vec{v}_1, \vec{v}_2, \vec{v}_3, \vec{v}_4, \vec{v}_5, \vec{v}_6)$?

- (i) Let

$$\vec{w} = \begin{bmatrix} 2 \\ 4 \\ 5 \end{bmatrix}$$

Is $\vec{w} \in \text{span}(\vec{v}_1, \vec{v}_2, \vec{v}_3, \vec{v}_4, \vec{v}_5, \vec{v}_6)$?