

Math 320 Linear Algebra Assignment # 12

1. Suppose that $A, B, C \in \mathbb{R}^{n \times n}$ with $A \sim B$ and $B \sim C$. Show that $A \sim C$.

2. Let

$$A = \begin{bmatrix} 14/3 & -5/3 & 1 \\ 17/3 & -8/3 & 1 \\ 1 & -1 & 2 \end{bmatrix}.$$

Consider:

$$\mathcal{B} = \left\{ \begin{bmatrix} 2 \\ 2 \\ 0 \end{bmatrix}, \begin{bmatrix} -1 \\ -1 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ 4 \\ 1 \end{bmatrix} \right\}.$$

(a) Show that \mathcal{B} is an eigenbasis with respect to A and find the corresponding eigenvalues?

(b) Find D and P so that $A = PDP^{-1}$.

3. Find an eigenbasis for

$$A = \begin{bmatrix} -3 & -3 & 6 \\ 0 & 0 & -6 \\ 0 & 0 & -3 \end{bmatrix}$$

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4. Consider the matrix

$$A = \begin{bmatrix} -13 & -10 & 5 \\ 20 & 17 & -10 \\ 10 & 10 & -8 \end{bmatrix}$$

(a) Find $\text{tr}(A)$

(b) Find $\det(A)$ (You can use an online calculator if you don't need more practice).

(c) Show $\text{char}(A) = -x^3 - 4x^2 + 3x + 18$ (the characteristic polynomial of A).

(d) Find the eigenvalues of A . (Hint: the eigenvalues are integers so you can find roots by graphing the polynomial)

(e) Find an eigenbasis for \mathbb{R}^3 with respect to A . (You can use an online row-reducing calculator unless you need more practice)

(f) Find invertible matrix P and diagonal matrix D so that $A = PDP^{-1}$.