

Problems from Assignment 11

1. Figure out what goes in this formula and prove it:

$$k \binom{n}{k} = n \binom{?}{?}.$$

2. Suppose that  $X \sim \mathcal{E}(\mu)$  with  $(\mu > 0)$ . Thus  $X$  has pdf:

$$f_X(x) = \begin{cases} \frac{1}{\mu} e^{-\frac{x}{\mu}} & x \geq 0 \\ 0 & x < 0 \end{cases}$$

(a) Show  $\int_{-\infty}^{\infty} f_X(x) dx = 1$

- (b) Find  $F_X(x)$  the cdf for  $X$ .

- (c) Show that  $X$  has the memory-less property, where if  $s, t > 0$  then:

$$P(X > s + t | X > s) = P(X > t)$$

3. Let  $X \sim \mathcal{G}(p)$  with  $(0 < p \leq 1)$ .

- (a) Let  $t$  be a positive integer find  $F_X(t)$ .

- (b) Let  $t$  be a positive integer find  $P(X > t)$ .

- (c) Show that the geometric distribution has the discrete version of the memory-less property, where if  $s, t$  are positive integers then:

$$P(X > s + t | X > s) = P(X > t)$$

- (d) Explain why this makes sense with the interpretation of the geometric distribution.