

## Table of Distributions

Name	PDF	Domain	Parameters	E	Var	MGF
Binomial	$\binom{n}{k} p^k (1-p)^{n-k}$	$0 \leq k \leq n$	$p \in (0, 1), n \in \mathbb{N}$	$np$	$np(1-p)$	$(1 - \theta + \theta e^t)^n$
Poisson	$\frac{\lambda^k}{k!} e^{-\lambda}$	$k \in \mathbb{N}$	$\lambda > 0$	$\lambda$	$\lambda$	$e^{\lambda(e^t - 1)}$
Normal	$\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$	$x \in \mathbb{R}$	$\mu \in \mathbb{R}, \sigma > 0$	$\mu$	$\sigma^2$	$e^{\mu t + \frac{\sigma^2 t^2}{2}}$
Gamma	$\frac{x^{r-1} \lambda^r}{e^{\lambda x} \Gamma(r)}$	$x > 0$	$r > 0, \lambda > 0$	$\frac{r}{\lambda}$	$\frac{r}{\lambda^2}$	$\left(1 - \frac{t}{\lambda}\right)^{-r}$
t	$\frac{\Gamma\left(\frac{n+1}{2}\right)}{\sqrt{n\pi}\Gamma\left(\frac{n}{2}\right)} \left(1 + \frac{x^2}{n}\right)^{-\frac{n+1}{2}}$	$x \in \mathbb{R}$	$t \in \mathbb{N}$	0	?	?
F	$\frac{\Gamma\left(\frac{m+n}{2}\right) m^{\frac{m}{2}} n^{\frac{n}{2}} w^{\frac{m}{2}-1}}{\Gamma\left(\frac{m}{2}\right) \Gamma\left(\frac{n}{2}\right) (n+mw)^{\frac{m+n}{2}}}$	$w > 0$	$m, n \in \mathbb{N}, ?$	?	?	?

Notes:

1. A binomial Random variable with  $n = 1$  is called a Bernoulli random variable.
2. A Gamma distribution with  $r = 1$  is call a Exponential random variable with rate  $\lambda$ .
3. If  $n \in \mathbb{N}$  then a Gamma distribution with  $r = \frac{n}{2}$  and  $\lambda = \frac{1}{2}$  is called a  $\chi_n^2$ -distribution.

Other Facts:

1. Suppose  $X_1, X_2, \dots, X_m \stackrel{\text{iid}}{\sim} N(\mu_X, \sigma^2)$  and are independent to  $Y_1, Y_2, \dots, Y_n \stackrel{\text{iid}}{\sim} N(\mu_Y, \sigma^2)$ . Let  $\bar{X}_m, \bar{Y}_n, S_X$ , and  $S_Y$  have their usual meaning. Then:

$$\frac{\bar{X}_m - \bar{Y}_n - (\mu_X - \mu_Y)}{S_p \sqrt{\frac{1}{m} + \frac{1}{n}}} \sim t_{m+n-2}$$

$$\text{where } S_p^2 = \frac{(m-1)S_X^2 + (n-1)S_Y^2}{m+n-2}.$$

2. Suppose  $X_1, X_2, \dots, X_m \stackrel{\text{iid}}{\sim} N(\mu_X, \sigma_X^2)$  and are independent to  $Y_1, Y_2, \dots, Y_n \stackrel{\text{iid}}{\sim} N(\mu_Y, \sigma_Y^2)$ . Then:

$$\frac{\bar{X}_m - \bar{Y}_n - (\mu_X - \mu_Y)}{\sqrt{\frac{S_X^2}{m} + \frac{S_Y^2}{n}}} \dot{\sim} t_\nu$$

where  $\nu$  is the closest integer to:

$$\frac{\left(\hat{\theta} + \frac{m}{n}\right)^2}{\frac{\hat{\theta}^2}{m-1} + \frac{1}{n-1} \left(\frac{m}{n}\right)^2},$$

$\hat{\theta} = \frac{S_X}{S_Y}$ , and  $\dot{\sim}$  means "approximately distributed as."

3. If  $A$  is an orthogonal  $n \times n$  matrix (i.e.  $A^T A = I_n$ ) and  $Z_1, Z_2, \dots, Z_n \stackrel{\text{iid}}{\sim} N(0, 1)$  and:

$$\begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_n \end{bmatrix} = A \begin{bmatrix} Z_1 \\ Z_2 \\ \vdots \\ Z_n \end{bmatrix}.$$

then:  $X_1, X_2, \dots, X_n \stackrel{\text{iid}}{\sim} N(0, 1)$ .