

1. Show every nonempty finite set of real numbers has a greatest element (i.e. if  $A$  is finite then  $\sup A \in A$ ). Hint: Prove by induction on  $m$  that if  $I_m \sim A$  then  $A$  contains a largest element.
2. Prove that if  $A \subseteq \mathbb{Z}$  and  $A$  is bounded from below then  $A$  has a least element (i.e.  $\inf A \in A$ ).