

1. Suppose  $f$  and  $g$  are differentiable on  $(a, b)$  and  $\lim_{x \rightarrow b^-} f(x) = 0$  and  $\lim_{x \rightarrow b^-} g(x) = 0$ . Also suppose that:

$$\lim_{x \rightarrow b^-} \frac{f'(x)}{g'(x)} = L$$

prove:

$$\lim_{x \rightarrow b^-} \frac{f(x)}{g(x)} = L.$$

2. Suppose  $f$  and  $g$  are differentiable on  $(a, b)$  and  $\lim_{x \rightarrow a^+} f(x) = +\infty$  and  $\lim_{x \rightarrow a^+} g(x) = +\infty$ . Also suppose that:

$$\lim_{x \rightarrow a^+} \frac{f'(x)}{g'(x)} = L$$

prove:

$$\lim_{x \rightarrow a^+} \frac{f(x)}{g(x)} = L.$$