

1. Show that if  $a, b \in \mathbb{R}$  then  $C(a + b) = C(a)C(b) - S(a)S(b)$ .
2. Show that  $S$  and  $C$  are periodic with period  $2\pi$  that is for all  $x$   $S(x + \alpha) = S(x)$  and  $C(x + \alpha) = C(x)$  is true for  $\alpha = 2\pi$  and does not hold for any  $0 < \alpha < 2\pi$ .  
Hint 1 : Show that if  $S(\alpha) = 0$  then  $S(\alpha - \pi) = 0$ . Hint 2 : Show  $C(\pi) = -1$ .
3. Show that  $S(x) = C(\frac{\pi}{2} - x) = -C(x + \frac{\pi}{2})$  and  $C(x) = S(\frac{\pi}{2} - x) = S(x + \frac{\pi}{2})$ .