

1. Let  $X$  be a non-empty set and for all  $x_1, x_2 \in X$  let  $d(x_1, x_2) = 0$  if  $x_1 = x_2$  and  $d(x_1, x_2) = 1$  otherwise. Show  $(X, d)$  is a metric space.
2. Show that if  $(V, \|\cdot\|)$  is a normed vector space then it is a metric space under  $d(v_1, v_2) = \|v_1 - v_2\|$ .
3. Show that  $\|\cdot\|_1$  is a norm on  $\mathbb{R}^n$  for all  $n$ .