

1. Use the well-ordering property to show that there does not exist an infinite strictly decreasing sequence of non-negative integers.
2. Like in chapter 7, let  $\mathbb{E} = \{\dots, -4, -2, 0, 2, 4, \dots\}$ .
  - (a) Write down the first 10 “primes” (positive elements in  $\mathbb{E}$  that are not the product of two elements in  $\mathbb{E}$ .)
  - (b) Make a conjecture about when a number in  $\mathbb{E}$  is prime. (Hint: There is a very simple condition.)
  - (c) Prove this conjecture.
3. Suppose  $p$  is prime and  $m > 0$  with  $p \nmid m$  then prove from the definition of gcd that  $\gcd(m, p) = 1$ .