

Non-Collected Problems:

1. Fill in the details of Gauss's divisibility lemma.
2. Determine if the following are Gaussian prime numbers, if not factor them into non-units.
 - (a) $5 + 3i$
 - (b) $7 + 0i$
 - (c) $1 - i$
 - (d) $4 + i$
 - (e) $2 + 4i$
 - (f) $4 - 5i$
3. For each of the following find a Gaussian prime that satisfies the conditions or explain why not such prime exists.
 - (a) $N(\pi) = 25$
 - (b) $N(\pi) = 125$
 - (c) $N(\pi) = 2$
 - (d) $N(\pi) = 17$
 - (e) $N(\pi) = 49$
4. Characterize all $k \in \mathbb{N}$ such that $N(\pi) = k$ for some Gaussian prime π .