## Additional Group Problems Assignment 19

1. Consider the group $D_{4}$ and the subgroup $C_{4}$.
(a) What is a simple way to describe the coset $V \cdot C_{4}$ in terms of $C_{4}$ (i.e. don't use the word "flip").
(b) Use this description to show that $V \cdot C_{4}=C_{4} \cdot V$
(c) Prove that if $G$ is a group and $H \leq G$ with $|G: H|=2$ then $H \unlhd G$.
2. (a) Let $G_{1}$ and $G_{2}$ be groups and suppose $e_{2}$ is the identity of $G_{2}$. Show that $G_{1} \oplus\left\{e_{2}\right\} \cong G_{1}$.
(b) Without proof just state a subgroup of $G_{1} \oplus G_{2}$ that is isomorphic to $G_{2}$.
