

SUMMARY OF VECTOR RELATIONS

	<i>Cartesian Coordinates</i>	<i>Cylindrical Coordinates</i>	<i>Spherical Coordinates</i>
Coordinate variables	x, y, z	r, \mathbf{f}, z	$r, \mathbf{q}, \mathbf{f}$
Vector representation, $\mathbf{A} =$	$\hat{\mathbf{x}}A_x + \hat{\mathbf{y}}A_y + \hat{\mathbf{z}}A_z$	$\hat{\mathbf{r}}A_r + \hat{\mathbf{f}}A_f + \hat{\mathbf{z}}A_z$	$\hat{\mathbf{r}}A_r + \hat{\mathbf{q}}A_q + \hat{\mathbf{f}}A_f$
Magnitude of \mathbf{A}, \mathbf{A}	$\sqrt{A_x^2 + A_y^2 + A_z^2}$	$\sqrt{A_r^2 + A_f^2 + A_z^2}$	$\sqrt{A_r^2 + A_q^2 + A_f^2}$
Position vector from origin to P_1, $\overline{OP_1} =$	$\hat{\mathbf{x}}x_1 + \hat{\mathbf{y}}y_1 + \hat{\mathbf{z}}z_1$ for $P(x_1, y_1, z_1)$	$\hat{\mathbf{r}}r_1 + \hat{\mathbf{z}}z_1$ for $P(r_1, \mathbf{f}_1, z_1)$	$\hat{\mathbf{r}}r_1$ for $P(r_1, \mathbf{q}_1, \mathbf{f}_1)$
Differential length, $dl =$	$\hat{\mathbf{x}}dx + \hat{\mathbf{y}}dy + \hat{\mathbf{z}}dz$	$\hat{\mathbf{r}}dr + \hat{\mathbf{f}}rd\mathbf{f} + \hat{\mathbf{z}}dz$	$\hat{\mathbf{r}}dr + \hat{\mathbf{q}}rd\mathbf{f} + \hat{\mathbf{f}}r\sin\mathbf{q}d\mathbf{f}$
Differential surface areas	$ds_x = \hat{\mathbf{x}}dydz$ $ds_y = \hat{\mathbf{y}}dxdz$ $ds_z = \hat{\mathbf{z}}dxdy$	$ds_r = \hat{\mathbf{r}}rd\mathbf{f}dz$ $ds_f = \hat{\mathbf{f}}drdz$ $ds_z = \hat{\mathbf{z}}rdrd\mathbf{f}$	$ds_r = \hat{\mathbf{r}}r^2\sin\mathbf{q}d\mathbf{q}d\mathbf{f}$ $ds_q = \hat{\mathbf{q}}r\sin\mathbf{q}drd\mathbf{f}$ $ds_f = \hat{\mathbf{f}}rdrd\mathbf{q}$
Differential volume, $dv =$	$dx dy dz$	$r dr d\mathbf{f} dz$	$r^2 \sin\mathbf{q} dr d\mathbf{f}$