Counterion crossbridges enable robust multiscale elasticity in actin networks

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Bundling and crosslinking of actin networks provide cells with tensile strength and mobility and play critical roles in diverse mechanical processes such as wounding healing and fertilization. One simple mechanism for bundling and crosslinking actin networks is using divalent counterions such as Mg$^{2+}$ to form crossbridges between actin filaments. Counterion crossbridges can also be exploited in materials engineering to alter the mechanics of polyelectrolyte materials. As such, the mechanical properties that counterion crossbridges confer to actin networks needs to be explored. Here, we use optical tweezers microrheology to characterize the mechanical response of actin networks in the presence of varying concentrations of Mg$^{2+}$. We couple mechanics to structure by using confocal microscopy to characterize the mobility and architecture of networks. We show that only modest bundling and network rearrangement is required to induce dramatic increases in the elasticity and stiffness of the networks. We further show that bundles are resilient to nonlinear forcing and exhibit surprisingly minimal dissipation above a critical counterion concentration. Finally, we demonstrate that while crosslinking of network fibers plays an important role in linear regime mechanics, filament bundling dictates the nonlinear response.

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I. INTRODUCTION

Semiflexible actin filaments are one of the most abundant biopolymers in the cytoskeleton, playing key roles in cell structure, adhesion, motility, and division [1]. Actin filaments are able to mediate these diverse mechanical processes and properties by forming entangled, crosslinked, and bundled networks with distinct mechanics and structures. For instance, networks of actin bundles comprise cellular structures such as stress fibers, filopodia, microvilli, and stereocilia; and enable mechanotransduction, fertilization, neuronal growth, and wound healing [2–4]. The unique bending stiffness, elasticity, and tensile strength of bundled networks confer the wide-ranging mechanical processes they enable [5,6]. While certain actin binding proteins (ABPs) can bundle actin filaments [4], due to the polyelectrolyte nature of actin, moderate concentrations of divalent ions, such as Mg$^{2+}$, are also sufficient to bundle actin and form connected networks of bundles via counterion crossbridges [6–9]. More generally, counterion crossbridges offer a simple mechanism to tune the stiffness and connectivity of a broad class of entangled biopolymer and polyelectrolyte networks.

Bundles of actin filaments are inherently stiffer than single filaments, such that a network of counterion-crossbridged filaments should have distinct mechanical properties from a network of single filaments [10]. For example, Mg$^{2+}$ concentrations of 10–50 mM have been reported to produce actin bundles with persistence lengths $l_p$ up to $\sim 4 \times$ larger than that of single actin filaments ($l_p \approx 10 \mu$m) [9,11–14]. Further, theoretical studies have shown that the bending stiffness of a bundle is impacted by both the number of filaments comprising the bundle as well as the density of connections the bundle has with its neighbors, suggesting that both bundling as well as crosslinking of bundles may play an important role in the mechanics of counterion-crossbridged networks [5].

Due to the physiological importance of counterion crossbridging, as well as its importance in addressing open questions in polymer physics, several studies have explored the structural properties of actin bundles and networks formed in the presence of Mg$^{2+}$ [2,6–9]. These studies have reported critical Mg$^{2+}$ concentrations of $\sim 10–25$ mM for the onset of bundling, but the extent to which bundle size and connectivity increases with increasing salt concentration above this threshold remains debated [2,9,15]. Two studies have reported that bundles assume a finite size that is insensitive to the concentration of actin and divalent salt [16,17] while another study reported a nonmonotonic dependence of bundle size on salt concentration, reaching a peak at 30 mM [9]. These findings are at odds with those from ABP-bundled actin network studies that reported a power-law increase in bundle size and stiffness with an increasing ABP:actin ratio.

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Nonetheless, several studies have probed the mechanical properties of actin networks bundled with fascin or varying mutants of \(\alpha\)-actinin [23] have been reported to stiffen at low \(R\) and soften at high \(R\) due to the rupturing of crosslinks that connected discrete bundles. These studies, as well as related simulation studies [24], have reported that the magnitudes of the frequency-dependent viscoelastic moduli \(G'(\omega)\) and \(G''(\omega)\) increased with increasing crosslinking, with all networks exhibiting a similar scaling of \(G'\) and \(G''\) with frequency that is unique from that of entangled networks. In the low-frequency regime, both \(G'\) and \(G''\) scale as \(\omega^{1/2}\). At intermediate frequencies, \(G' > G''\) with \(G'\) exhibiting an \(\omega\)-independent plateau while \(G''\) reaches a local maximum followed by a minimum. In the high-frequency limit, \(G' > G''\) with both moduli exhibiting power-law scaling with exponents of \(-0.5\)–1. While the high-frequency limit has been predicted to reflect the dynamics of single filaments or bundles, the low-\(\omega\) regime displays the rheology of the connected network. The extent to which these mechanical properties translate to counterion-connected networks remains unknown. While the transient nature of ABP crosslinkers has been suggested to be primarily responsible for the mechanics described above, it is unclear if counterion crossbridges exhibit similar plasticity and nonequilibrium dynamics.

Here, we use optical tweezers microrheology and confocal microscopy to characterize the linear and nonlinear mechanical response as well as the mobility and architecture of entangled actin networks in the presence of varying concentrations of Mg\(^{2+}\). To probe the nonlinear force response, we optically drag a microsphere through the network and measure the resulting force the network exerts on the sphere during and after the strain [25]. To measure the linear response, we track the thermal fluctuations of trapped microspheres to quantify the frequency-dependent viscoelastic moduli \(G'(\omega)\) and \(G''(\omega)\). We couple these measurements with laser scanning confocal microscopy experiments to characterize the effect of Mg\(^{2+}\) on the network microstructure and rigidity.

We show that modest increases in salt concentration (2–52 mM) lead to dramatic changes in the mechanical response—with network stiffness, nonlinear force response, elasticity, and relaxation timescales all increasing by an order of magnitude or more. Unlike actin networks crosslinked by ABPs, counterion-bundled networks exhibit a nearly complete elastic response with essentially no dissipation. While such extreme behavior is typically expected to arise from dramatic changes to the network architecture, we instead find that the induced bundling and crosslinking results in relatively small changes to the mesoscopic structure of the network. We also show that while crosslinking of network fibers plays an important role in linear regime mechanics, filament bundling—which only occurs above a critical salt concentration—dictates the nonlinear response.

## II. Materials and Methods

### A. Sample Preparation

Alexa-568-labeled actin (A-12373, Life Technologies) and unlabeled actin monomers (Cytoskeleton, Inc.) were stored at \(-80^\circ\text{C}\) in G-buffer (2 mM Tris pH 8.0, 0.5 mM DTT, 0.1 mM CaCl\(_2\)). To form networks, thawed Alexa-568-actin and unlabeled G-actin were mixed at a 1:10 molar ratio to a final concentration of 5.8 \(\mu\text{M}\) in 100 mM K-Pipes pH 7.0, 2 mM EGTA, 1 mM ATP, and varying concentrations of MgCl\(_2\) (2, 4, 14, 27, or 52 mM). A trace amount of Alexa 488-BSA-coated polystyrene microspheres (Polysciences, Inc.) of 4.5 \(\mu\text{m}\) in diameter was added for microrheology measurements (Fig. 1). The solution was pipetted into a microscope sample chamber comprised of double-sided tape as a spacer between the slide and coverslip, sealed with epoxy, and incubated for 1 h at room temperature. The predicted mesh size of the network is \(\xi = 0.3/e^{1/2} = 0.6 \mu\text{m}\), where \(e\) is the actin concentration in mg/mL.

### B. Microrheology

We used an optical trap setup built by outfitting an Olympus IX71 fluorescence microscope with a 1064-nm Nd:YAG fiber laser (Manlight) focused with a 60\(^\times\) 1.4 numerical aperture (NA) objective, as described and validated previously [25,26]. A position-sensing detector (First Sensor) measured the laser deflection, which is proportional to the force exerted on a trapped microsphere by the network. The trap stiffness was calibrated via Stokes drag in water and passive equipartition methods [27]. The laser deflection was recorded at a rate of 20 kHz using custom-written LABVIEW programs. Custom MATLAB scripts were used for postacquisition data analysis. All presented data are averages of 20 trials using 20 different beads each at a different location in the sample chamber.

For linear microrheology measurements [Fig. 1(c)], \(G'(\omega)\) and \(G''(\omega)\) were extracted from the thermal fluctuations of an optically trapped bead (recorded for 180 s) using the generalized Stokes-Einstein relation as described in Ref. [28]. Briefly, the normalized mean-squared displacement of the ensemble of trapped beads \(\Pi(\tau) = \langle \Delta r^2(\tau) \rangle/2\tau^2\) is computed, from which the Fourier transform of \(\Pi(\tau)\), \(\hat{\Pi}(\omega)\), is computed via the relationship [28]

\[
-\omega^2 \hat{\Pi}(\omega) \frac{\Pi(\tau)}{\tau_1} (1 - e^{-i\omega\tau_1}) + \hat{\Pi}_\infty e^{-i\omega\tau_N}
+ \sum_{k=2}^{N} \left( \frac{\Pi_k - \Pi_{k-1}}{\tau_k - \tau_{k-1}} \right) (e^{-i\omega\tau_{k-1}} - e^{-i\omega\tau_k}),
\]

where \(\hat{\Pi}_\infty\) is the slope of \(\Pi(\tau)\) extrapolated to infinite time and \(\tau_N\) is the \(N\)th lag time. The complex modulus \(G'(\omega) = G'\omega/\Pi(\omega) + iG''(\omega)\) is then determined using \(G'(\omega)\).}

For nonlinear microrheology [Fig. 1(d)], a piezoelectric nanopositioning stage (Mad City Laboratories) displaced an optically trapped bead 5 \(\mu\text{m}\) relative to the sample chamber at a speed of 20 \(\mu\text{m/s}\) while measuring the resulting force the network exerted on the trapped bead during (0.25 s) and after...
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FIG. 1. Experimental approach to elucidate the effect of countercion crossbridges on the mechanics and structure of entangled actin networks. (a) Cartoon of networks of single actin filaments at low [MgCl₂] (left) and networks of bundles at high [MgCl₂] (right). (b) Projection of 900 frames of a representative time series of 5.8-μM actin networks with [MgCl₂] listed. Time series were captured at 15 fps using a Nikon A1R confocal microscope and QImaging CCD camera. (c), (d) Optical tweezers microrheology measurements showing sample measured force traces (black) and stage position (red) for (c) linear microrheology determined from thermal fluctuations of a trapped bead, and (c) nonlinear microrheology in which the bead is displaced 5 μm at 20 μm/s (strain) after which the force is recorded for an additional 30 s (relaxation). Data shown are for a network with 14 mM MgCl₂.

C. Microscopy

Time-series and three-dimensional image stacks (z-stacks) of networks were collected using a Nikon A1R laser scanning confocal microscope with a 60×1.4 NA objective and QImaging CCD camera [Fig. 1(b)]. The 512×512 pixel time-series was recorded at 15 fps for 60 s. The z-stacks comprised 100 images with 0.2-μm spacing. Using Fiji, the projection of the mean intensity of each pixel of each time-series or z-stack, averaged over frames or z, respectively, was computed to produce the 512×512 projection images [Fig. 1(b)].

III. RESULTS AND DISCUSSION

To characterize the impact of counterion concentration on the mechanical response of actin networks, we first evaluate the frequency-dependent linear viscoelastic moduli, \( G'(\omega) \) and \( G''(\omega) \). As shown in Fig. 2, \( G'(\omega) \) and \( G''(\omega) \) for all networks display a similar frequency dependence: \( G' \) exhibits a slow rise at low frequencies followed by a frequency-independent elastic plateau \( G_0 \) [Fig. 2(b)] while \( G'' \) initially
scales as $\sim \omega^{2/5}$ at low frequencies, followed by a local maximum, after which it scales as $\sim \omega^{7/8}$ [Fig. 2(c)]. Further, $G' > G''$ for most of the frequency regime, but all curves exhibit a crossover to $G' > G''$ at high frequencies. These general features are markedly similar to those reported for actin networks crosslinked by ABPs such as $\alpha$-actinin [29], indicating that bundle connectivity via crosslinking plays an important role in the mechanical response. While the frequency dependence displayed in Fig. 2 is similar for all networks, the magnitudes of $G'$ and $G''$, as well as the time $\tau_c = 2\pi / \omega_c$ at which the crossover to $G' > G''$ occurs, depends strongly on $[\text{Mg}^{2+}]$.

The magnitude of $G_0$ increases as $[\text{Mg}^{2+}]$ increases from 2 to 52 mM, following a power-law relation $G_0 \sim [\text{Mg}^{2+}]^{3/5}$. At the lowest salt concentration (2 mM) we expect minimal bundling and crosslinking as this is the standard concentration used when realizing entangled solutions of single actin filaments. Indeed, we find that $G_0$ for 2 mM $\text{Mg}^{2+}$ is comparable to the theoretically predicted value $G_0 \approx kT / \xi^{1/5} l_p^{1/5} \approx 0.01$ Pa for a 5.8-μm entangled actin solution [30]. However, as $\text{Mg}^{2+}$ increases we expect crosslinking and bundling via counterion crossbridges to occur [7,8]. Thus, to estimate the expected dependence of $G_0$ on $[\text{Mg}^{2+}]$, we turn to the predicted scaling of $G_0$ with persistence length $l_p$ for a crosslinked actin network $G_0 \sim l_p^{-1/5}$ [24]. If we consider the previously reported persistence lengths for salt-induced actin bundles ($\sim 4 \times l_p$ of a single actin filament), then we expect $G_0$ to increase $\sim 16$-fold from the value for an entangled actin solution. This predicted value of $\sim 0.16$ Pa is quite close to our measured value $G_0 \approx 0.17$ Pa for 52 mM $\text{Mg}^{2+}$.

We also evaluate the crossover time $\tau_c = 2\pi / \omega_c$, which indicates the timescale at which the dynamics of single filaments or bundles, rather than the connected network, dictates the mechanics [31]. For entangled polymers $\tau_c$ is a measure of the predicted entanglement time $\tau_c$ while for crosslinked networks $\tau_c$ is related to the relaxation rate of single fibers in the network [10]. For the lowest $\text{Mg}^{2+}$ concentration, we measure $\tau_c \approx 0.46$ s, which is comparable to the predicted entanglement time for our system $\tau_c \approx \beta \xi^{1/5} l_p^{1/5} \approx 0.25$ s, where $\xi$ is the friction coefficient. The crossover time decreases with increasing $\text{Mg}^{2+}$ and for $[\text{Mg}^{2+}] > 2$ mM follows the scaling $\tau_c \sim [\text{Mg}^{2+}]^{-1/4}$. As previously predicted [5], as bundles become stiffer and more connected they exhibit extended elastic regimes, pushing the high-frequency scaling regime to higher frequencies, i.e., lower $\tau_c$ values. Together our linear response results suggest that both increased connectivity (crosslinking) and increased persistence length (bundling) of actin fibers enables the strongly elastic response displayed for high salt networks in the linear regime. To determine the extent to which this salt-induced elasticity exhibited in the linear regime is robust to nonlinear forcing, we turn to our nonlinear microrheology results.

We previously found that nonlinear strains were sufficient to break biotin-NeutAvidin crosslinks in actin networks, leading to stress yielding, plasticity, and stress dissipation [32]. In contrast, as shown in Fig. 3, we find that both the magnitude and slope of the induced force increase substantially with increasing $[\text{Mg}^{2+}]$ with no signs of dissipation. Only the lowest salt conditions ($\leq 4$ mM) exhibit yielding to a primarily viscous (strain-independent) plateau regime, whereas for $[\text{Mg}^{2+}] \geq 14$ mM the force continues to increase nearly linearly, reaching values $\sim 7$-fold larger than for low salt conditions [Fig. 3(c)]. Similarly, following the strain, the force the network exerts on the bead dissipates nearly completely for low salt conditions as the network relaxes back.
As shown, networks display stress-stiffening above a critical MgCl\textsuperscript{2+} concentration. Above this concentration, the networks exhibit sustained elasticity for the duration of the 30-s relaxation phase dropping by less than a factor of 2/3, whereas the highest salt concentration exhibits no signatures of crosslinking. Thus, bundle formation, which stiffens network fibers, rather than crosslinking that connects bundles exhibits only 2%, compared to a 10-fold drop for networks below concentrations well below the upper bound of this range are sufficient.

We also evaluate the magnitude of \( K \) when it reaches peak stiffness \( K_{\text{max}} \) and terminal stiffness \( K_t \) as well as the time at which each of these occurs, \( t_{\text{stiff}} \) and \( t_{\text{soft}} \), respectively. Above the critical bundling concentration, these parameters are surprisingly unaffected by changes in [Mg\textsuperscript{2+}], suggesting that bundling may contribute an "all-or-nothing" effect to nonlinear mechanics—either suppressing bending and dissipation or not. Previous studies on the size and stiffness of Mg\textsuperscript{2+}-induced bundles have reported similar insensitivities or nonmonotonic dependences on salt concentration [7–9,16]. One explanation for this insensitivity, as described in Ref. [16], is that beyond a critical bundle thickness, further increases in salt concentration instead promote the formation of junctions between distinct bundles as well as branching of bundles into separate connected bundles. The net result is that as salt increases, the density of connections between bundles continuously increases (via junctions and branching) while the bundle thickness remains fixed.

The timescales \( t_{\text{stiff}} \) and \( t_{\text{soft}} \) can shed further light on the mechanisms driving the nonlinear mechanics exhibited. The average measured values are \( t_{\text{stiff}} \approx 4 \text{ ms} \) and \( t_{\text{soft}} \approx 0.2 \text{ s} \). We previously showed that highly entangled actin networks stress-stiffen over a time comparable to the fastest predicted relaxation time for actin networks, the mesh time \( \tau_{\text{mesh}} \), whereas softening occurs over a time comparable to the entanglement time \( \tau_e \) [30]. For entangled actin at 5.8 \( \mu \text{M}, \tau_{\text{mesh}} \approx \beta \zeta \xi^{-4/p} \approx 0.026 \text{ s} \) and \( \tau_e \approx 0.25 \text{ s} \). However, as above, if we consider that bundles increase \( l_p \) by \( \sim 4 \times \), then we can estimate \( \tau_{\text{mesh}} \approx 6.5 \text{ ms} \) and \( \tau_e \approx 0.19 \text{ s} \), which are remarkably close to our measured timescales \( t_{\text{stiff}} \) and \( t_{\text{soft}} \). These collective results indicate that in the nonlinear regime networks above \( c_b \) behave as entangled networks of stiff fibers with no signatures of crosslinking. Thus, bundle formation, which stiffens network fibers, rather than crosslinking that connects fibers, plays the dominant role in the increased stiffness and elasticity in response to nonlinear forcing. Conversely, as described above, the linear response (Fig. 2) appears to be dictated primarily by crosslinking with bundling playing a secondary role.

We next turn to the force relaxation \( F_R \) following strain to determine the extent to which the network can alleviate stress over time (Fig. 5). For networks below \( c_b, F_R \) follows a power-law decay with an exponent of \( \sim 0.3 \), quite close to previously reported nonlinear microrheology results for entangled actin [25]. However, above \( c_b \) networks exhibit very little relaxation with \( F_R \) dropping by less than a factor of 2 (i.e., \( F_{R,0}/F_{R,0} > 0.5 \)) over the entire 30-s relaxation phase [Fig. 5(b)]. In fact, for the highest [Mg\textsuperscript{2+}] the force drops by only 2%, compared to a 10-fold drop for networks below elastic response over the entire strain rather than yielding to a mostly viscous regime (Figs. 4(c) and 4(d)] suggests that the filaments cannot disentangle and rearrange themselves to alleviate stress. Crosslinking and bundling would prevent this source of dissipation seen in entangled actin networks [33].
FIG. 5. Force relaxation of actin networks following nonlinear strain is suppressed by counterion-induced bundling. (a) Force relaxation $F_{R}$ shown in Fig. 3(b), normalized by the force immediately following the strain $F_{R,0}$ for MgCl$_2$ concentrations listed in the legend. The black line represents power-law scaling with the exponent listed. (b) The ratio of the force reached at the end the relaxation phase $F_{R,f}$ to the initial force $F_{R,0}$ as a function of [MgCl$_2$]. $F_{R,f}/F_{R,0} = 1$ for a completely elastic system while $F_{R,f}/F_{R,0} = 0$ for a system with complete dissipation. (c) The relaxation timescale $t_{\text{relax}}$, defined as the time required for the force to decay to 68.3% of the initial value $F_0$, increases over two orders of magnitude as [MgCl$_2$] exceeds the critical bundling concentration $c_b$. This extreme mechanomemory and elasticity is much stronger than reported in previous studies on crosslinked actin networks, which all show plasticity and dissipation [32,34].

We also compute the time for networks to start alleviating stress, which we quantify as the time $t_{\text{relax}}$ at which the force drops to 68.3% of its value immediately following strain ($F_{R,0}$). As shown, $t_{\text{relax}}$ for networks below $c_b$ is quite close to the predicted mesh time $\tau_{\text{mesh}} \approx 0.026$ s, suggesting that below $c_b$ neither bundling nor crosslinking is pervasive or strong enough to contribute to the nonlinear response. However, as [Mg$^{2+}$] becomes larger than $c_b$, $t_{\text{relax}}$ increases by two to three orders of magnitude. These timescales are on the order of previously reported values of $\sim 10$ s for the disengagement time (i.e., the time for an entangled filament to reptate out of its confining tube) for entangled actin [35]. This agreement suggests that the very limited dissipation that does occur in bundled networks following nonlinear forcing is likely via reptation of bundled fibers. As such, it appears that it is bundling rather than crosslinking that is so effective

$c_b$. This extreme mechanomemory and elasticity is much stronger than reported in previous studies on crosslinked actin networks, which all show plasticity and dissipation [32,34].

FIG. 6. Increasing concentrations of Mg$^{2+}$ induce crosslinking and bundling in actin networks. Images shown are mean intensity projections of time-series (left) and z-stacks (right) of fluorescent-labeled actin networks acquired using a Nikon A1R laser scanning confocal microscope with 60× 1.4 NA objective and QImaging CCD camera. Each row corresponds to a different MgCl$_2$ concentration as listed in the corresponding right panel. Each time-series image is a projection of 900 images collected at 15 fps for 60 s while each z-stack is a projection of 100 images separated in z by 0.2 $\mu$m. The insets are 3× zoom-ins of each network. Time-series projections show a continuous decrease in network mobility while z-stacks show a discrete shift from networks of single filaments to bundled networks for concentrations above 4 mM MgCl$_2$. 

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at suppressing nonlinear relaxation modes and thus conferring mechanomemory. To connect the intriguing mechanics described above with the network structure and mobility we collect time-series and three-dimensional image stacks (z-stacks) of fluorescent-labeled networks using laser scanning confocal microscopy as described in Sec. II C. In the time-series projections shown in Fig. 6, networks with more Brownian fluctuations of mobile filaments should exhibit more gray pixels (lower contrast) and appear more uniform (lower pixel-to-pixel variation), whereas rigid networks should show more black and white (higher contrast) and structure (larger pixel-to-pixel variation). Similarly, z-stack projections for networks of bundled filaments manifest as more black and white pixels and structure, whereas networks of single filaments have lower contrast and more uniformity. As shown, for concentrations below $c_b$, networks appear to be comprised almost entirely of single “floppy” filaments that have ample Brownian fluctuations whereas networks above $c_b$ appear to be more rigid and comprised largely of bundles of filaments. However, upon closer inspection there is a notable difference in the concentration dependence for projections of time-series versus z-stacks. Time-series projections show a steady increase in contrast and structure as $[\text{Mg}^{2+}]$ increases, similar to our linear regime results (i.e., $G_0$, $t_c$) that display a power-law dependence on $[\text{Mg}^{2+}]$ (Fig. 2). On the other hand, z-stack projections exhibit an “all-or-nothing” effect similar to our nonlinear microcirculation results, i.e., $K_{\text{max}}$, $K_r$, $t_\text{relax}$, $F_{R,i}/F_{R,0}$ (Figs. 3 and 4). Namely, contrast and pixel-to-pixel variation do not appear to increase proportionally with $[\text{Mg}^{2+}]$, rather there is a notable structural shift between networks above and below $c_b$, but little variation in contrast and structure is seen between networks that are either above or below $c_b$. Recall that time-series are sensitive to mechanisms that suppress temporal fluctuations such as crosslinking of filaments or bundles, whereas z-stacks are only sensitive to structural changes such as bundling. As such, our imaging results directly support our argument that the linear rheology is most sensitive to crosslinking density, which continuously increases with increasing $[\text{Mg}^{2+}]$. Conversely, the nonlinear mechanics are dictated largely by the increased stiffness of bundles which appears to saturate soon after reaching the critical concentration—providing the all-or-nothing effect seen.

Finally, it is important to point out that given the dramatic effect of $[\text{Mg}^{2+}]$ on the linear and nonlinear mechanics, the variations in images are surprisingly small. Typically, large changes to rheological properties are accompanied by mesoscale changes to the network structure whereas here...
modest microscale bundling and crosslinking appear to be sufficient.

To further quantify the Mg$^{2+}$-dependent structural changes seen in Fig. 6 and corroborate our argument above, we evaluate the probability distribution of intensity values for the time-series and z-stack projections (Fig. 7). As shown, for $[\text{Mg}^{2+}] > c_b$, the intensity distributions for both time-series and z-stack projections are broader than for networks below $c_b$, with higher low-intensity values and larger high-intensity tails. These features demonstrate that high-Mg$^{2+}$ conditions ($[\text{Mg}^{2+}] > c_b$) indeed produce multifilament bundles that are brighter and less mobile than single filaments (high-intensity tails) and the apparent voids in the network are more static and empty (higher low-intensity probabilities). We quantify these features by determining the intensity values for each distribution at a threshold probability value of $10^{-4}$ (∼1% of the peak probability $P_{\text{max}}$, shown in insets of Fig. 7). Figures 7(a) and 7(b) show that for 52 mM Mg$^{2+}$ the low-intensity threshold values (“Low I”) are 32% and 29% lower than for 2 mM Mg$^{2+}$ in time-series and z-stack projections, respectively. Likewise, the high-intensity threshold values (“High I”) are 46% and 30% higher for 52 mM Mg$^{2+}$ compared to 2 mM Mg$^{2+}$.

The broader the distribution (more dark and light pixels), the lower the peak probability value must be, so evaluating $P_{\text{max}}$ quantifies this counterion-dependent breadth. To best visualize variations in $P_{\text{max}}$, as well as the width of the distributions, we rescale the distributions such that their peaks align [Figs. 7(c) and 7(d)]. Upon rescaling we see that indeed the peak heights decrease as the counterion concentration increases, with $P_{\text{max}}$ values that are 30% and 53% lower for 52 mM Mg$^{2+}$ than for 2 mM Mg$^{2+}$ in time-series and z-stack projections, respectively.

However, the more dramatic feature is the variation in high-intensity tails in time-series compared to z-stack projections. For time-series projections the high-intensity tails steadily increase with increasing $[\text{Mg}^{2+}]$ while for z-stack projections the tails for networks below $c_b$ (2 and 4 mM) collapse to a single value, as do two of the three networks above $c_b$ (14 and 27 mM). This effect is in line with what we would expect for a time-series compared to z-stacks if the density of crosslinking increased steadily with $[\text{Mg}^{2+}]$ while the transition to bundling was discrete. As described above and suggested in Ref. [16], one mechanism that could allow for such an effect is the increasing density of junctions and branching between growing bundles. Namely, as $[\text{Mg}^{2+}]$ increases, bundles initially grow thicker until they reach a finite width, presumably occurring at $c_b$. At the same time the frequency of bundle-bundle junctions and bundle branching events, both of which are effectively crosslinking events, increases. However, after reaching $c_b$, a further increase in $[\text{Mg}^{2+}]$ only serves to increase the density of junctions and branching nodes. The net effect on mechanics is a continuously increasing contribution from crosslinking yet a discrete all-or-nothing contribution from bundling as $[\text{Mg}^{2+}]$ increases.

IV. CONCLUSIONS

Actin bundling and crosslinking provides cells with tensile strength and mobility and plays critical roles in diverse mechanical processes such as mechanotransduction and division. One simple mechanism cells utilize to bundle and crosslink actin is to use divalent counterions to form crossbridges between actin filaments. Counterion crossbridges can also be exploited in materials engineering to tune the stiffness and connectivity of biopolymer and polyelectrolyte networks. However, the impact of counterion crossbridges on the mechanics of actin networks had yet to be investigated.

Here, we have addressed this need by using optical tweezers to characterize the linear and nonlinear mechanical response of entangled actin networks in the presence of varying concentrations of Mg$^{2+}$. We have shown that above a critical counterion concentration $c_b$, bundle formation enables networks to exhibit stress-stiffening and robust elasticity that can sustain nonlinear forcing. Unlike the discrete shift seen in the nonlinear response, in the linear regime the apparent stiffness and elasticity of the network increases steadily with increasing $[\text{Mg}^{2+}]$, owing to the counterion-enabled crosslinking of actin filaments and bundles. Notably, these mechanical changes are significantly stronger than those previously reported for actin crosslinked or bundled via ABPs.

To corroborate these results and connect mechanics to structure, we performed laser scanning confocal microscopy experiments to characterize the effect of Mg$^{2+}$ on the network microstructure and rigidity. Our results confirm that increasing counterion concentration serves to continuously increase the crosslinking density while inducing a discrete phase change to bundled fibers above a critical concentration. Importantly, we have also shown that networks exhibit surprisingly modest changes to the structure and mobility given the striking changes in the mechanical response that counterion crossbridges enable.

Our collective results not only provide key insights into understanding diverse cellular processes but also inform industrial applications. We further hope that our intriguing results will spark theoretical investigations to model the effect of counterion crossbridging on the mechanical response of biopolymer and polyelectrolyte networks.

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