

1. Find q, r with $0 \leq r < a$, so that $b = a \cdot q + r$ with:
 - (a) $a = 683097, b = 3121328$
 - (b) $a = 613257, b = -1835521$.
 - (c) $a = 36856, b = 28794$.
 2. Compute the following:
 - (a) $25309 \% 8428$
 - (b) $41443955 \% 525486$
 3. Without a calculator find the last digit of: $5745 \cdot 21448 + 9465 \cdot 18163 + 1839 \cdot 88418$.
 4.
 - (a) Without a calculator determine the remainder of 55873593339 when it is divided by 9.
 - (b) Is 55873593339 divisible by 9?
 5. Encipher the message “tube” using an affine cipher with key $a = 3$ and $b = 16$.
 6. (Wait until Wednesday to try this problem.) Find the inverse of 8 (mod 29) (that is, find c such that $8c \equiv 1 \pmod{29}$).
- Do one of the following two problems, you can do both for extra credit.**
7. Prove that if $a \equiv b \pmod{m}$ and c is an integer then $a + c \equiv b + c \pmod{m}$. You will use both the definition of mod and divisibility.
 8. Prove that if $d|a$ and $d|b$ then $d|a + b$ and $d|a - b$.
 9. Find the following places on campus and take a picture of yourself there and send it to me.
 - (a) The Math Learning Center
 - (b) The Logic Center
 - (c) The Writing Center