# The art of model fitting to experimental results (Supplementary Information)

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#### 1. Notes on the use of *fitteia* interfaces

*fitteia* (Fitting Environment Interfaces for All) provides a set of graphic user interfaces accessible through the internet using any web browser (e.g. IE, Opera, Firefox, Mozilla, Safari, Chrome). fitteia is presently available on the site http://fitteia.org. *fitteia* platform allows for:

- 1 The graphical representation of experimental results and/or mathematical functions;
- 2 The numerical fit of arbitrary user defined linear and/or non-linear functions dependent on M fitting parameters and n-experimental variables to experimental data
- 3 The data treatment using an integrated programmable calculator
- 4 The use of a integrated Matlab-like calculator
- 5 The writing of professional-quality reports using LaTeX
- 6 The production of documents in PDF, PNG, JPG, EPS formats using the fit results
- 7 The user registration through a email/password security process to assure the user's privacy
- 8 The sharing of working areas with other select users
- 9 The sharing of user defined fitting functions/fitting models, documents/projects with other select users
- 10 The possibility to use three different expertise levels (e.g. Basic, Advanced, Expert)
- 11 The saving/recovery of important results
- 12 The download/upload of the configuration/setup files
- 13 The assignment of two levels of user privileges

#### 1.1. Registration

The *fitteia* login webpage (http://fitteia.org) presents some basic information about the service and presents a "login" link that users must follow to login the system. New users must first register accessing the "*sign up*" page. A valid email address is required to "*sign up*" *fitteia*. The user receives an email with a new password after answering a security question. This password is required to proceed to the second step of the registration process. The user is invited to change the password and to introduce his name in the system.

Registered users may reset their passwords following the same procedure.

#### 1.2. Logging in

Logging in the system requires typing the email used for the registration and the password. When logging in for the first time the user is directed to a webpage as presented in the print screen of Fig. 1. Some links will conduct to actions that are more



Figure 1. *fitteia* webpage after logging in.

or less self-explaining. The user should check the information concerning the "Browser Support".

- "**Tutorial1**" is the name of a default folder that contains some self-explaining fit and plot examples.
- "browser" allows for a vista to the users home folder tree using the web browser.
- "manage" links to a webpage where the user can delete files or include emails of other users with whom the folder will be shared provided that the folder's name is not a duplicate of a pre-existing folder of the guest user.

"Tutorial1" links to *fitteia*'s *fitter* module that opens with some pre-recorded data loaded, as partially presented in Fig. 2.

1.3. The fitter module

# 1.3.1. Header

<b>fitteia</b> new.fitteia.user@gmail.com HD used quota: 676 kB/5 MB (13.5%). <u>Clean</u> ? <u>Need more</u> ?	News   Help   Basic   Advanced   Expert   Calculator   Plotter   Report Editor   Upload   MyFits   Logout
Overwrite         //Tutorial1         //file_name         Archive           (/folder_name/file_name Don't use spaces, or non-characters)         Image: Contract of the space of the	list SPL-ELISA    Recover Download

Figure 2. *fitteia*'s *fitter* webpage header.

Besides the self-evident links the following links deserve some additional comments.

- "News" links to a page where new *fitteia* features are presented after being included in the system.
- "Basic", "Advance", and "Expert" link to *fitter* module interface with different layouts according to the level of expertise required by the system to tackle the user's data analysis problem.

- "Calculator" links to a programable calculator that receives the fitting parameters of the last fit performed and helps the user to perform additional calculus.
- "Plotter" links to *fitteia*'s *plotter* module.
- **Report Editor**" links to a web form filled with the last fit results and can be used to prepare LATEX reports
- "**Upload**" links to a upload web form that allows the user to upload a file to the system. usually a previous downloaded *fitter* or *plotter* environment file.

"MyFits" links to the list of user folders (included folder shared with him).

In Fig. 2 a pair of text boxes can be found between buttons "Overwrite" and "Archive". The text box filled with "Tutorial1" shows the folder's name where the user is working. Additional folders can be created by changing this name. Next to it a text box filled with "file\_name" shows the environment name given to file where all the web page information will be saved.

- "Overwrite" saves the web form in a file named "file\_name.sav" in folder "Tutorial1" This file can be overwritten repeatedly.
- "Archive" saves the web form in a file named "file\_name-YYYY-MM-DD\_hh:mm:ss.sav" in folder "Tutorial1". This file can not be overwritten and can only be deleted in "MyFits->Folder\_name->manage".

On the bottom right side of Fig. 2 it is possible to see a button to select a previous saved environment fit data file to "Recover" or "Download". The list of files can be filtered using the "list" button.

#### 1.3.2. Data, Plot Settings and Fitting Function

The core of the *fitter* module webpage is composed by the sections with following characteristics:

"1°-Data" The main text box allows the user to type (or copy and paste) values of x, y, and  $\epsilon_y$ , where x is the independent variable, y is the dependent variable, and  $\epsilon_y$  is expected to be the uncertainty of y. The numbers must be written in three columns and separated by white spaces. The values x, y, and  $\epsilon_y$  form column vectors, named "c1", "c2",...,"cn", where 1,...,n is the order of the column

Below the main "Data" text box a second box allows users to perform arithmetic operations with the column vectors of the "Data" text box. The syntax for the arithmetic calculations is that of PERL but it is quite simple to write expressions to perform basic calculations. Both " $^{"and}$  "\*\*" can be used in power expressions (e.g. c1 $^{p}$  or c1\*\*p).

**abs(c1)** – absolute values of column vector c1;

sqrt(c1) – square root function of column vector c1;

 $\exp(c1)$  – exponential function,  $e^{c1}$ ;

sin(c1), cos(c1), tan(c1), asin(c1), acos(c1), atan(c1) - trigonometric functions of column vector c1; sinh(c1), cosh(c1), tanh(c1), asinh(c1), acosh(c1), atanh(c1) - hyperbolic
functions of column vector c1;

Button "Calculate" when be used evaluates these expressions in sequence and generates a new Data table.

Button "Data Plot" generates a new layout of the *fitter* webpage where a graph with a data plot is presented according to the "Plot Parameters" introduced.

- "2°-Plot Parameters" Axis names, limits, tick names, etc.. can be defined in this section. Both x and y autoscaling is possible.
- "3°-Function and Parameters" The function to be fitted to the experimental results must be written in language C. The names of the independent and dependent variables must be introduced and they will have the corresponding values of the first and second columns of the "Data" table when performing the leastsquares' minimization. For the large majority of cases the only language C specific mathematical functions that users must be aware of are:

fabs(x) – absolute value of a floating point number x;

 $pow(x,y) - x^y;$ 

sqrt(x) – square root function,  $\sqrt{x}$ ;

exp(x) – exponential function,  $e^x$ ;

sin(x), cos(x), tan(x), asin(x), acos(x), atan(x) – trigonometric functions;

sinh(x), cosh(x), tanh(x), asinh(x), acosh(x), atanh(x) – hyperbolic functions;

For conditional calculations the syntax "(condition) ? if\_true\_this : if\_false\_this" can be used. When calculating ratios between integers, like in the case of "1/2" it is required to write "1.0/2.0" to obtain the expected value 0.5 as the result, otherwise an integer devision is performed and the result is 0.

If the fitting function is composed of different terms, *ftteia*'s *fitter* specific syntax character "+" can be used to allow for the independent plotting of each one of the terms of the fitting function. The "Plot Parameters" section layout is changed according to the number of terms of the fitting function to allow for the setting of lines types, colors and labels of each curve.

Button "Compile" will compile the function and link it with the *fitteia*'s fitter kernel. A link to a log file might help to debug the function in case compilation errors occur. The *fitter* webpage layout changes in the case of a successful compilation and below the page header a graph and the function parameters' table are shown next to each other.

In the Data tex box and in the text boxes containing the plot settings addition arithmetic expressions can be included and will evaluated when the web form is submitted to the *fitteia* server.

#### 1.3.3. Recovering a previous fit

After selecting the name and recovering the fit the *fitter* webpage layout shows the graph with the data and the function parameters' table as illustrated in Fig. 3 for the



fit file "Basic-EJP-Resonance-const-err-2013-08-09\_19-13-54".

Figure 3. *fitteia*'s *fitter* graph and function parameters' table after "Recover" a previously saved fit.

If the user has still storage space in his account buttons "Fit" and "Plot" are seen below the function parameters' table. They allow for two different actions:

- "Fit" starts the fitting procedure using the values of the fitting parameters in the table as initial values. If a fitting parameter status is "Free" the minimization procedure tries to find the minimum of  $\chi^2$  in the parameter's space defined by the user. If "Min" and "Max" have finite values for a given parameter the minimization is restricted to that particular region of the parameter's space, otherwise the region extends  $[-\infty; \infty]$ . The graph is updated with both data points and the fitting curves calculated using the fitting output values.
- "Plot" generates a graph with the data points and the curves calculated using the values of the parameters without performing a fitting procedure. It can be used to generate curves calculated with different parameters.

When the fitting ends an additional column is added to the function parameters' table with either the error estimates of the "Free" parameters, or the word "Fixed" stating the status of that parameter during the minimization procedure, as illustrated in Fig. 4

Below the graph several links become handy when exporting the graph in different file formats, getting an automatic PDF report of the fit, obtaining a table with the values of the theoretical curves, or a LATEX table with the fitting results.

"fit.log" deserves a comment as it contains a log report of the MINUIT actions during the fitting procedure plus some information from the *fitteia*'s *fitter* module. "PDF Report" links to the "Report Editor" previously referred and returns a PDF report that contains the graph and fitting results obtained (check below some examples).



Figure 4. fitteia's fitter graph and function parameters' table after a fitting procedure.

#### 1.4. Using the Calculator module

After a fit the function parameters obtained are exported to the *Calculator* module. The *Calculator* web form layout shows a text box area where the user can write equations and expressions and perform different types of calculations including tables and/or vector operations. By default *Calculator* starts with a list of examples that can be studied as a tutorial text. In Fig. 5 part of *Calculator* webpage is illustrated after opening the "example" operations' set previously saved. The fitting parameters obtained in the fit of Fig. 4 were loaded and simple calculations using those parameters are presented.

#### 1.5. Plotter module

Producing more elaborated graphs can be achieved using *fitteia*'s *Plotter* module. When opened it presents a basic layout. After "recovering" a previous save example its layout is modified as illustrated in Fig. 6.

The particular example illustrated in Fig. 6 presents 7 data sets where one data set is shown with black circles and the reaming data sets are represented by lines. The settings of each data set are of the type shown in Fig. 7 for Data set 1.

#### 1.6. Advanced and Expert modes

Using the notes presented above for the *fitteia*'s Basic user mode the behavior of the *fitter* module for the remaining user modes can be followed using the examples illustrated in the "Tutorial1" folder.

fitteia.user@gmail.com           HD used quota: 1304 kB/5 MB (26.1%). Clean? Need more?			
Save as list *	example  Copen Download Delete		
Examples   General math   Trig. functions   Units' factors: f.p.n.u.m.k.M.G.T   Text area 12 Calculate     Clear   Clear all   Reload	x $\overline{60}$ Fitting parameters on memory m = 1.02190e-01		
f:=1/(2*pi)*sqrt(K/m) f	K = 1.03591e+01 l = 1.62600e-01		
<pre>&gt; ans=1.60242 m+0.01 &gt; ans=0.11219</pre>	F0 = 3.66734e-02		
m=ans > m=0.11219 f			
<pre>&gt; ans=1.52934 f=1/(2*pi)*sqrt(K/m)</pre>			
Calculate Clear all Reload	2		

Figure 5. *fitteia*'s *Calculator* layout example.



Figure 6. *fitteia*'s *Plotter* layout example.

#### 1.7. Use of fitteia with increased privileges

For advanced model fitting the basic functions writing is, some times, not enough as new complex functions might be required. If they are not included in the system a user can ask for additional privileges in order to be able to develop more elaborated functions and libraries. The only difference noticed by the users is the layout of the *fitter* module as it includes additional text boxes for the additional user's C code. In Fig. 7 is presented one example of the *fitter* web age layout of section "Function and

The art of model fitting to experimental results (ESI)

Units' factors: fp.n.u.m.k.M.G.T) Font size: 100 %	Data (Show ÷)				
	Data Show +				
T L'OMMONT LING					
# Three columns: x y ey Da	Data Set type xydy \$				
# plotif 1,10					
1.14085 201.19 14.1841	Symbol circle				
1.16181 205.126 14.3222					
1.18278 207.012 14.3879	Line none + black + 2.0 Straight +				
1.20374 207.893 14.4185	T abat				
1.22471 212.008 14.5605	Laber				
1.24568 213.758 14.6204	black the DOS X' DOS Y'				
1.26664 215.416 14.6771	String Diack + pos x. pos y.				
1.28761 217.813 14.7585	(Use "" to add different strings and/or scale coordinates)				
1.30857 222.189 14.906	MyPlot Auto Plot				
1.32954 224.866 14.9955					
1.35051 227.209 15.0735					
1.37147 232.29 15.2411					
1.39244 236.109 15.3658					
1.4134 238.855 15.4549					
1.43437 243.356 15.5999					
1.45533 246.647 15.705					
1.4763 249.055 15.7815					
t commont lines shout with "#"					
# check the Calculate How To just below					
" oneen ene carcarace non re jube berow					
Calculate1 Calculate How To?					

Figure 7. *fitteia*'s *Plotter* layout example of plot setting for one data set.

Parameters".

3°- Function and Parameters (Specific function's library)			
Variables:	1st ind. x 2nd ind. z dep. y		
Parameters	tau1,E1,Ar0,Ar1,Ar2,A,S0,Tc,gama,n,d,r,ED,D345,tau3,E3,A0,A1,A2,fcm0,fcm1,fcM0,		
AuxCode Editor:	on ÷ Go		
User function declarations	double ECD_poli(),BPP(),BPPfT(), TorreyfT(), ECDfT(), ODFNfT(), RWoessner(),OPFfTiso()		
Function (written in C)       y=RWoessner(x,z,tau3,tau1,S0,Tc,gama,Ar0,Ar1,Ar2,E3,E1,Tci,A)\+TorreyfT(x, z,d, r, n,r*r*1e-20/(6*0345),ED,Tci)\+0PFfTiso(x,z, A0,A1,A2,f01,Tci,fcm0, fcm1,fcM0,fcM1,np)			
(one line only, use "\+" instead of "+" if you want to plot each contribution separatly)			
Additional C code double BPPfT(double x,double z, double a, double tau0, double Ea,double Tr { double tau, af, BPP(); if(z>1e3){ tau=tau0*exp(Ea/8.31*(1.0/x-1.0/Tref)); af=BPP(z,a,tau); } else{ tau=tau0*exp(Ea/8.31*(1.0/z-1.0/Tref)); af=BPP(x,a,tau); } entrum of			
	} double TorreyfT(double x,double z, double d, double r, double n, double tau0, double Ea, double Tref) {		
Compile the function. Co	mpiled without errors: log file		

**Figure 8.** *fitteia*'s *fitter* layout example of section "Function and Parameters" for a privileged user.

#### 2. Notes on the NMR relaxation models

#### 2.1. Translational self-diffusion

The relaxation model used to fit spin-lattice relaxation results of a liquid crystal compound is in many cases that developed by H. C. Torrey [1] and can be expressed as

$$\left(T_1^{-1}\right)_{\rm SD} = \frac{9}{8}\gamma^4 \hbar^2 \left(\frac{\mu_0}{4\pi}\right)^2 \frac{n\tau_D}{d^3} \left[\mathcal{T}(\alpha, \omega\tau_D) + 4\mathcal{T}(\alpha, 2\omega\tau_D)\right],\tag{1}$$

with  $\mathcal{T}(\alpha, x)$  given by

$$\mathcal{T}(\alpha, x) = \frac{32\pi\alpha}{15x^2} \left[ \left( u_+ \left( 1 + \frac{1}{u_-^2 + u_+^2} \right) + 2 \right) e^{-2u_+} \cos u_- \right. \\ \left. + u_+ \left( 1 - \frac{1}{u_-^2 + u_+^2} \right) + u_- \left( 1 - \frac{1}{u_-^2 + u_+^2} \right) e^{-2u_+} \sin 2u_- \right]$$
(2)

where

$$u_{\pm} = \frac{1}{2} \left( \frac{q(1\pm q)}{\alpha} \right)^{1/2} \tag{3}$$

$$q = \frac{x}{\left(4 + x^2\right)^{1/2}} \tag{4}$$

and  $\alpha = \langle r^2 \rangle / (12d^2)$ . In this model *n* is the density of spins, *d* is distance between neighborhood molecules,  $\langle r^2 \rangle$  is the mean square jump distance, and  $\tau_D$  is the average time between molecular translational jumps.

#### 2.2. Order parameter fluctuations

In the isotropic phase of a liquid crystal compound, close to the phase transition into the nematic phase, fluctuations of the order parameters are some times observed [2] when analyzing spin-lattice relaxation results. The relaxation mechanism can be expressed bt

$$\left(T_1^{-1}\right)_{OPF} = \frac{A_{OPF}}{\omega^{1/2}} \int_{\omega_{Cl}/\omega}^{\omega_{Ch}/\omega} \frac{\sqrt{x}}{1 + (x + \omega_0/\omega)^2} dx \tag{5}$$

with  $A_{OF} = (9/8)(\mu_0/4\pi)^2 \gamma^4 \hbar^2 k_B T \eta_{iso}^{1/2}/(4\pi^2 K_{iso}^{3/2} a_{eff}^6)$ .  $\omega_{Cl}$  and  $\omega_{Ch}$  are the low and high cut-off frequencies that correspond to the largest and smallest wave length modes, respectively.  $\omega_0 \sim K_{iso}/\eta\xi^2$  depends on the coherence length associated with the size of nematic cybothatic domains in the isotropic phase and acts also as a cut-off frequency [2].

#### References

- H. C. Torrey. Nuclear spin relaxation by translational diffusion. *Physical Review*, 92(4):962–969, 1953.
- [2] R.Y. Dong. Nuclear magnetic resonance of liquid crystals. Springer New York, 1997.

# 3. *fitteia*'s *fitter* reports corresponding to the examples presented in the paper

<i>fitteia</i> F	lepo	$\mathbf{rt}$
(internet based	fitter :	service)

Subject	oject Tutorial1, Basic-EJP-Elastic-Constant			
Date	Friday 9 <sup>th</sup> August, 2013, 20:30			
Affiliation	pj.sebastiao@gmail.com 77.54.10.14			
Abstract	Fit report produced with the fit results of function: $y=g/K^*x + d0$ to the 12 experimental points, considering 2 free parameters.			
$ \begin{array}{c c} g = 9.8 \ (\text{fixed}) \\ K = 9.9356 \pm 0.17085 \end{array}  d0 = -0.00062389 \pm 0.001344 \\ \end{array} $				
	$\chi^2[1] = 2.22217 \qquad \chi^2_t = 2.22217$			
(m)	0.10 0.08 0.06 0.04 0.02 0.02 0.02 0.04 0.02 0.02 0.04 0.06 0.06 0.06 0.06 0.06 0.06 0.06 0.06 0.06 0.06 0.06 0.02 0.02 0.04 0.06 0.02 0.02 0.04 0.02 0.02 0.04 0.02 0.02 0.04 0.02 0.02 0.04 0.02 0.02 0.02 0.02 0.04 0.02 0.02 0.02 0.04 0.02 0.02 0.02 0.04 0.02 0.02 0.02 0.04 0.06 0.08 0.10			

recta.pdf

fitt	eia I	Repo	$\mathbf{rt}$	
internet	based	fitter	service	)

Subject	Tutorial1, Basic-EJP-Damped-oscilator		
Date	Friday 9 <sup>th</sup> August, 2013, 20:30		
Affiliation	pj.sebastiao@gmail.com 77.54.10.14		
AbstractFit report produced with the fit results of function: $Z=(Zt0-Zinf)^*exp(-l^*t) + Zinf$ to the 24 experimental points, considering 3 free parameters.			
	$l = 0.12878 \pm 0.0044065 = 7im f = -0.0022205 \pm 0.00002744$		
$Zt0 = 0.10319 \pm 0.0015956$			
	$\chi^2[1] = 30.1509 \qquad \chi^2_t = 30.1509$		



Subject	Subject Tutorial1, Basic-EJP-Resonance-const-err				
Date	Friday 9 <sup>th</sup> August, 2013, 20:31				
Affiliation	pj.sebastiao@gmail.com 77.54.10.14				
Abstract	Fit report produced with the fit results of function: A=F0/(m*sqrt(pow(K/m-4*pi*pi*fa*fa, 2.0) + 16*pi*pi*l*l*fa*fa)) to the 26 experimental points, considering 3 free parameters.				
	$ \begin{array}{ll} m = 0.10219 \mbox{ (fixed)} & l = 0.1626 \pm 0.0026012 \\ K = 10.359 \pm 0.0055152 & F0 = 0.036673 \pm 0.00035622 \end{array} $				
	$\chi^2[1] = 84.5677 \qquad \chi^2_t = 84.5677$				
	$ \begin{array}{c} 0.12\\ 0.10\\ 0.08\\ \hline 0.08\\ \hline 0.06\\ 0.04\\ \hline 0.04$				
	0.02 - 0.00 -				
	A.pdf				

*fitteia* Report (internet based fitter service)



Subject	Tutorial1, Basic-EJP-Phase-const-err		
Date	Friday 9 <sup>th</sup> August, 2013, 20:40		
Affiliation	pj.sebastiao@gmail.com 93.108.109.5		
Abstract	Fit report produced with the fit results of function: y=(x>sqrt(K/m)/(2*pi))? (atan $(2*1*2*pi*x/(K/m-4*pi*pi*x*x))$ + pi + b)*180/pi (atan $(2*1*2*pi*x/(K/m-4*pi*pi*x*x))$ + b)*180/pi to the 23 experimental points, considering 3 free parameters.		
	$m = 0.10219 \text{ (fixed)} \qquad l = 0.12442 \pm 0.012487$ $K = 10.269 \pm 0.022925 \qquad h = 0.32068 \pm 0.019616$		
	$\chi^2[1] = 8.5947 \qquad \chi^2_t = 8.5947$		
۵(dearee)	200 - 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		
	recta.pdf		

*fitteia* Report (internet based fitter service)

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Subject	Tutorial1, Expert-EJP-spring-ma	2355	
Date	Pate Friday 9 <sup>th</sup> August, 2013, 20:24		
Affiliation	ion pj.sebastiao@gmail.com 77.54.10.14		
Abstract Fit report produced with the fit results of function: $y=(flag==1) ? g/K^*x + d0 : (flag==2) ? (Zt0-Zinf)^*exp(-l^*x) + Zinf : (flag==2) ? F0/m/sqrt(pow(K/m-4*pi*pi*x*x, 2.0) + 16*pi*pi*1*l^*x*x) : (x>sqrt(K/m)/(2*2*pi*x/(K/m-4*pi*pi*x*x)) + pi + a0)*180/pi : (atan(2*l*2*pi*x/(K/m-4*pi*pi*x*x)) + pi + a0)*180/pi : (atan(2*l*2*pi*x/(K/m-4*pi*pi*x*x)) + a0)*180/pi to the 85 experimental points, considering 8 free parameters.$			
	g = 9.8 (fixed)	$A = 0.64014 \pm 0.09051$	
	m = 0.10219 (fixed)	$Zt0 = 0.1045 \pm 0.00058394$	
	$K = 10.392 \pm 0.0076501$	$Zinf = -0.0024616 \pm 0.0002795$	
	$d0 = 0.0027261 \pm 0.00028868$	$a0 = 0.33976 \pm 0.019833$	
	$l = 0.14291 \pm 0.00077808$	$F 0 = 0.032980 \pm 0.00029400$	
	$\chi^{2}[2] = 31.0108$ $\chi^{2}[4] = 10.327$ $\chi^{2}_{t} = 60.8831$	$\chi^2[1] = 8.73329$ $\chi^2[3] = 10.8119$	
0.10 -	(a)	0.10 (b) m=0.102 kg	
€ 0.06		_ 0.06 - "\$	
⊿I(n			
0.04	-	0.04 - ~~~ -	
-	-	- Xe -	
0.02		0.02	
0.00	 0.02 0.04 0.06 0.08 0.10 m(kg)	0.00 - 5 - 10 - 5 - 20 - 25 - 10 - 15 - 20 - 25 - 10 - 15 - 20 - 25 - 10 - 15 - 20 - 25 - 10 - 15 - 20 - 25 - 10 - 15 - 20 - 25 - 10 - 10 - 10 - 10 - 10 - 10 - 10 - 1	
	Spring-Mass-1.pdf	Spring-Mass-2.pdf	

*fitteia* Report (internet based fitter service)



Subject	Tutorial1, Basic-EJP-x-rays		
Date	Friday 9 <sup>th</sup> August, 2013, 20:21		
Affiliation	pj.sebastiao@gmail.com 77.54.10.14		
Abstract	Fit report produced with the fit results of function: $y=a + a0^{*}exp(-pow((q-q0)/b0, 2.0)) + a1^{*}exp(-pow((q-q1)/b1, 2.0)) + a2^{*}exp(-pow((q-q2)/b2, 2.0)) + a3^{*}exp(-pow((q-q3)/b3, 2.0))$ to the 69 experimental points, considering 13 free parameters.		
$\begin{array}{c cccc} a = 153.21 \pm 5.4086 & a2 = 200 \pm 29.723 \\ a0 = 252.52 \pm 15.052 & b2 = 4 \pm 0.12931 \\ b0 = 1 \pm 0.014206 & q2 = 10.419 \pm 0.12791 \\ q0 = 2.4294 \pm 0.040112 & a3 = 300 \pm 9.6683 \\ a1 = 93.836 \pm 7.8405 & b3 = 2.3904 \pm 0.14258 \\ b1 = 1.7183 \pm 0.29467 & q3 = 14.164 \pm 0.080498 \\ q1 = 4.7695 \pm 0.14836 & q3 = 14.164 \pm 0.080498 \end{array}$			
$\chi^2[1] = 8.78204 \qquad \chi_t^2 = 8.78204$			
(1 E)	700 600 400 400 200		

*fitteia* Report (internet based fitter service)

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Subject	Tutorial1, Expert-EJP-5CB_Iso		
Date	Friday 9 <sup>th</sup> August, 2013, 20:26		
Affiliation	pj.sebastiao@gmail.com 77.54.10.14		
Abstract	$ \begin{array}{l} \label{eq:stars} \hline \mbox{Fit report produced with the fit results of function:} \\ z=( \ (y>500.0) \ ? \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $		
	$Arot = 5.7688 \times 10^{+08} \pm 8.45 \times 10^{+06}$ $tauS = 1.45 \times 10^{-09} \text{ (fixed)}$ ES = 29412  (fixed) $tauL = 3.36 \times 10^{-10} \text{ (fixed)}$ $EL = 46828 \pm 6860.6$ d = 5  (fixed) $n = 4.59 \times 10^{+22} \text{ (fixed)}$ r = 4  (fixed)	$Dref = 5.44 \times 10^{-11} \text{ (fixed)}$ $ED = 32800 \text{ (fixed)}$ $Tref = 313 \text{ (fixed)}$ $Aopf = 17438 \pm 1017.9$ $f0 = 1 \times 10^{+05} \text{ (fixed)}$ $fcM = 4.25 \times 10^{+07} \text{ (fixed)}$ $fcm = 6.838 \times 10^{+05} \pm 99853$ $np = 10 \text{ (fixed)}$	
$\chi^{2}[313] = 8.81902 \qquad \chi^{2}[1 \times 10^{+08}] = 0.184233$ $\chi^{2}_{t} = 9.00325$			
5 a) NMF 4 - - - - - - - - - - - - -	R @ 100MHz	$10^{3}$ b) NMR @ (313K) 40°C $10^{2}$ b) NMR @ (313K) 40°C	

*fitteia* Report (internet based fitter service)